

MHD simulations of turbulent galactic outflows

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Project A4 within CRC 1491

“Magnetohydrodynamical halos of starforming galaxies”

- 1 Observations: R.-J. Dettmar, M. Stein → (talk by MS)
 - 2 **Theory / numerics**: H. Fichtner, JK → this talk)
- **Goal**: study **turbulence** properties of galactic outflows.

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- **Goal**: study **turbulence** properties of galactic outflows.
- **Method**: MHD + “fluid-like” equations for turbulence

$$Z^2 = \langle \delta u^2 + \delta b^2/n \rangle, \quad \sigma_c = 2 \langle \delta \vec{u} \cdot \delta \vec{b} / \sqrt{n} \rangle / Z^2, \quad \lambda_{\text{corr}}$$

from **Reynolds averaging**: $\vec{B} = \langle \vec{B} \rangle + \delta \vec{b}$, $\vec{u} = \langle \vec{u} \rangle + \delta \vec{u}$

- Significant **synergy effects** from recently completed similar work on (inner) heliosheath (with S. Oughton, U Waikato).

Starting from what we know...

Adopted strategy

Start from (working) **solar wind setting**, then gradually move towards galactic winds, changing one thing at a time:

- 1 spherical to cylindrical **coordinates** (same physics)
- 2 wind source: sphere \rightarrow disk(-like surface)
- 3 first HD, then MHD, then MHD + turbulence

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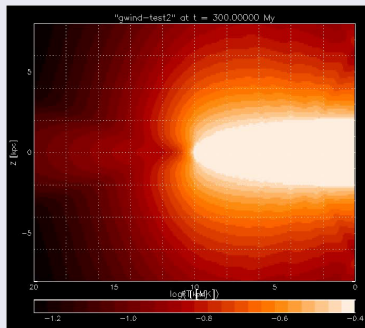
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- 1 spherical to cylindrical **coordinates** (same physics)
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- “disk” surface: prolate **ellipsoid** with semi-axes $\rho_{\text{core}}, z_{\text{core}}$
 - initial conditions and $\Phi_{\text{grav}}(\vec{r})$ given in terms of

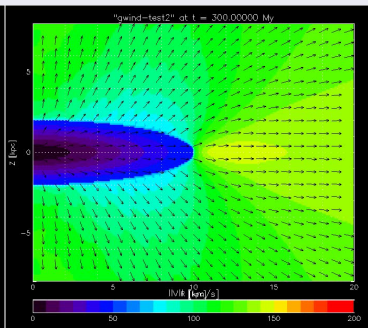
$$R_e(\rho, z) := \sqrt{(\rho/\rho_{\text{core}})^2 + (z/z_{\text{core}})^2}$$

- \Rightarrow inner “disk” boundary at $R_e = 1$
recovering spherical case if $\rho_{\text{core}} = z_{\text{core}}$

HD sample run (adiabatic, $T_0 = 0.5$ MK, $n_0 = 1$ cm $^{-3}$)



temperature $\log(T)$

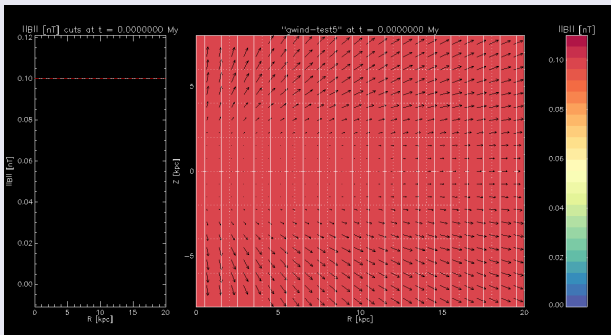


velocity $\|\vec{u}\|$

Global parameters:

$$\rho_{\text{core}} = 10 \text{ kpc}, z_{\text{core}} = 2 \text{ kpc}, \gamma = 5/3, \mu = 0.62$$

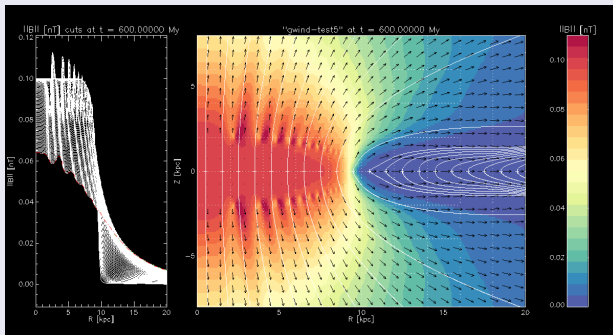
MHD sample run ($\vec{B}|_{t=0} = 0.1 \text{ nT } \vec{e}_z$)



field strength $\|\vec{B}\|$ + field lines (white)

- keep $\vec{u} = \vec{0}$ inside ellipsoid to maintain $\nabla \cdot \vec{B} = 0$

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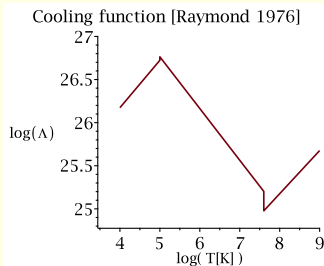
field strength $\|\vec{B}\|$ + field lines (white)

- keep $\vec{u} = \vec{0}$ inside ellipsoid to maintain $\nabla \cdot \vec{B} = 0$
- “ripple” artifacts caused by finite cell size ($\sim 0.1 \text{ kpc}$); can be eliminated by smoothing the boundary.

Reference benchmark: *"Dynamical Behavior of Gaseous Halo in a Disk Galaxy"* [Habe & Ikeuchi 1980]

- uses standard hydro(!) equations in 2D plus "cooling" term

$$\partial_t \mathbf{e} = \dots - (nm)^2 \Lambda(T)$$



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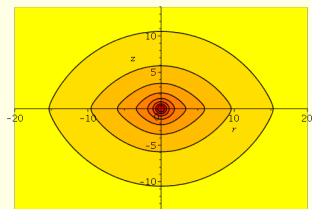
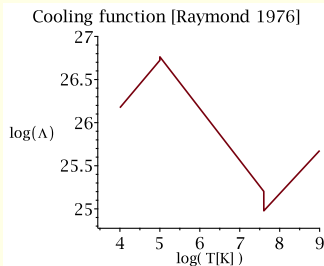
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$$\Phi_d = - \sum_{i=1}^2 \frac{GM_i}{\sqrt{\rho^2 + \left(a_i + \sqrt{z^2 + b_i^2} \right)^2}}$$

[Miyamoto & Nagai 1975]



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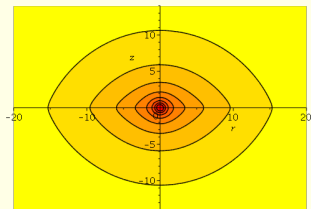
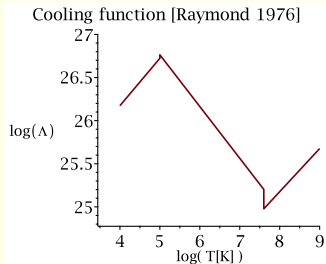
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[Miyamoto & Nagai 1975]

- spherical halo potential [Innanen 1973]:

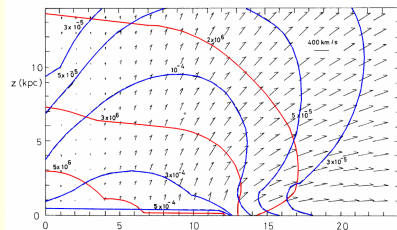
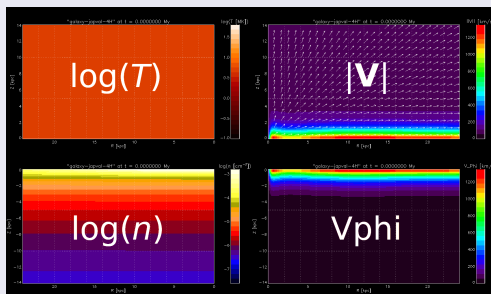
$$\Phi_h \propto \ln(1 + r/r_0) + (1 + r/r_0)^{-1}$$

- boundary cond.s at $z = 0$, $\rho \in [4, 12]$:
 T and n fixed, $u_\varphi = \sqrt{(\partial_\rho \Phi_{\text{tot}}) \rho}$



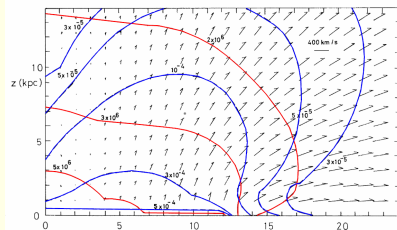
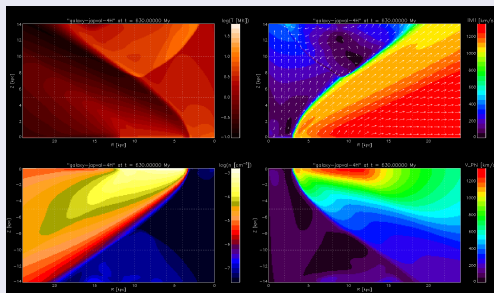
Target work

H&I '80 "wind-type" model
 ($T_d = 5$ MK, $n_d = 10^{-3}$ cm $^{-3}$,
 $\Phi_h \neq 0$). Right plot: **density** and
temperature at $t = 200$ My.

Data from Cronos validation run ($\rho \in [4, 10]$ boundary)

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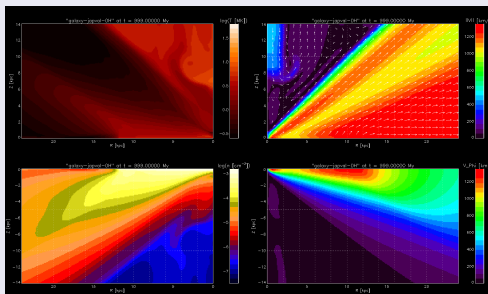
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Note that
 $|u_\varphi|$ is too
 large ($\sim 5x$)

Determining the cause of the near-axis inflow instability

- Closing the "hole" in the disk makes no (big) difference.

Data from Cronos validation run ($\rho \in [0, 10]$ boundary)

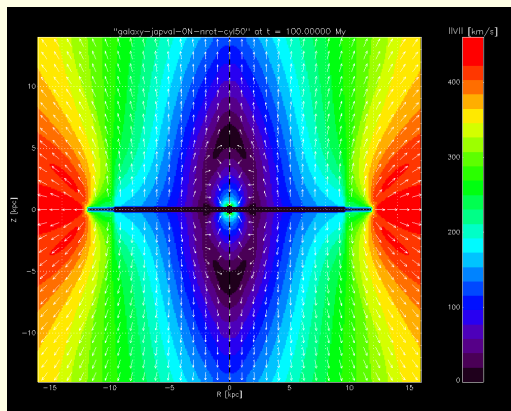


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- Numerical **issues at $\rho = 0$** ?

Poloidal cut of $\|\vec{v}\|$

...at $t = 100$, $\Omega = 0$,
on a **cylindrical** grid
(where $\rho = 0$ is a
grid boundary)

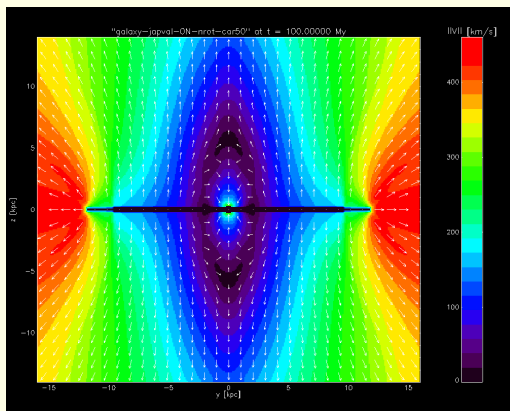


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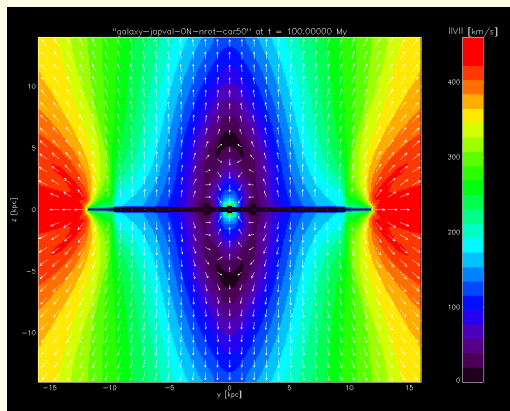


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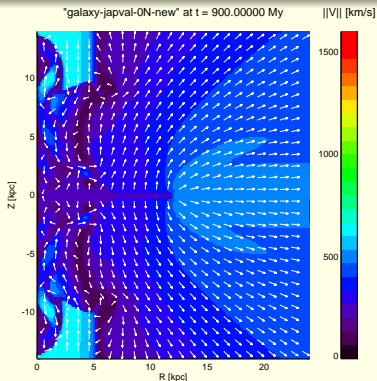
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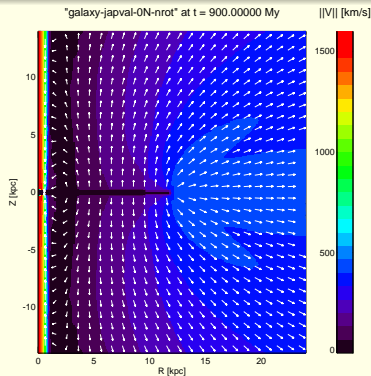


Determining the cause of the near-axis inflow instability

- Closing the "hole" in the disk makes no (big) difference.
- Numerical issues at $\rho = 0$? No, same on Cartesian grid.
- **Rotation?** Still unstable, but it does widen the inflow region.



$$\Omega(\vec{r}) = \Omega_{\text{Kepl}}(\vec{r})$$



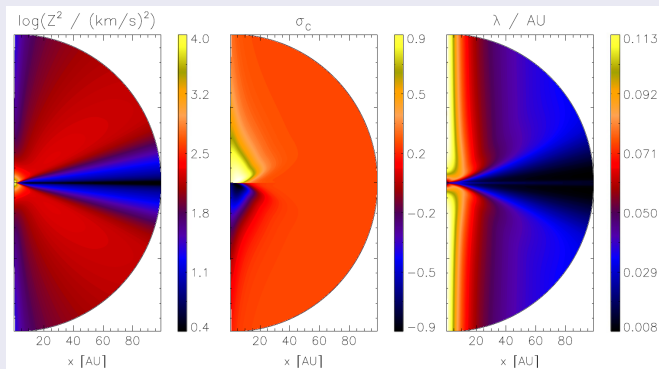
$$\Omega(\vec{r}) = 0$$

Preliminary conclusion

- Crucial distinction: only **massive** galaxies exhibit the instability. (Trial run for M82 reaches steady-state.)
- Miamoto-Nagai potential has $M_1 + M_2 \approx 27 \cdot 10^{10} M_{\odot}$ (likely based on the Milky Way).
- Starburst galaxies of interest typically are less massive, e.g. $M = (0.9 \dots 8.6) \cdot 10^{10} M_{\odot}$ [Stein+2023]

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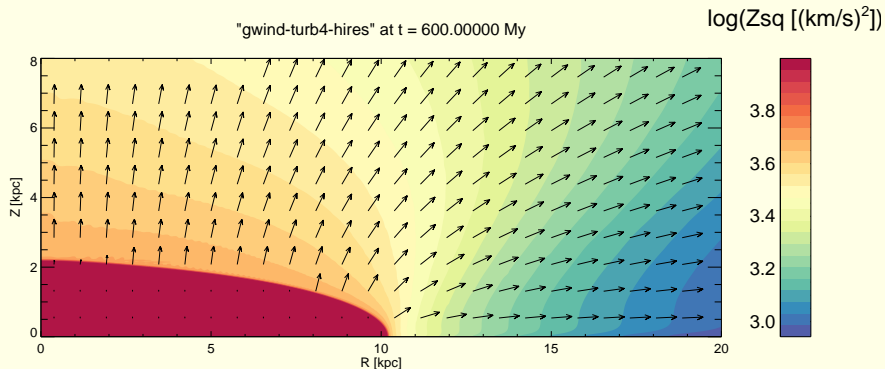
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- Starburst galaxies of interest typically are less massive, e.g. $M = (0.9 \dots 8.6) \cdot 10^{10} M_\odot$ [Stein+2023]
- Stationarity seen by Habe & Ikeuchi [1980] might be an **artifact** of low grid resolution ($N_\rho \times N_z = 22 \times 30$).

Turbulence quantities in the solar wind ($\varphi = \text{const. cuts}$)

[Wiengarten+2015]

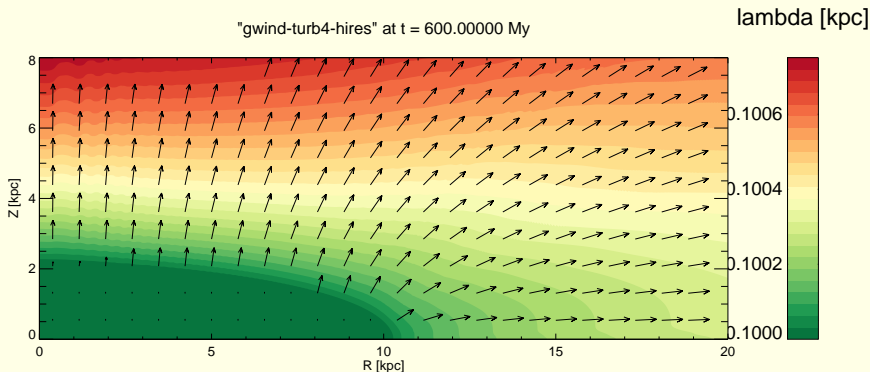
- Z^2 first decreasing with r , then constant
- $|\sigma_c|$ decreasing (note polarity change with hemisphere)
- λ approx. constant along polar axis

Turbulence seen in (first) galactic wind simulations



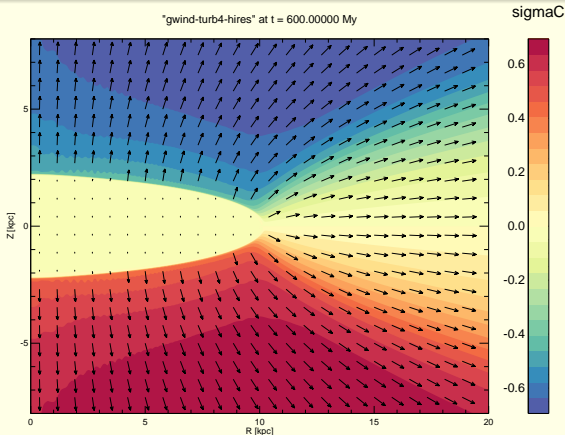
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Turbulence seen in (first) galactic wind simulations



- Z^2 decreasing with r (but smaller dynamic range)
- λ essentially constant
- $|\sigma_c|$ **increasing** from zero(!) (but with polarity change)

Summary and outlook

- A numeric single-fluid (ideal) **MHD+turbulence model** for a galactic wind is established and tested.
- Origin of axial **flow instability** traced to galaxy's mass (\Rightarrow likely not relevant for starburst galaxies in **A4**).
- 2D patterns of **turbulence** in Z^2, σ_c, λ generated (from which $\delta\vec{u}$ and $\delta\vec{b}$ can be found/constrained).

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Imminent next steps:

- Further analysis of differences to heliospheric case
- Then, ready to use “realistic” (= **observationally** inspired) parameters.

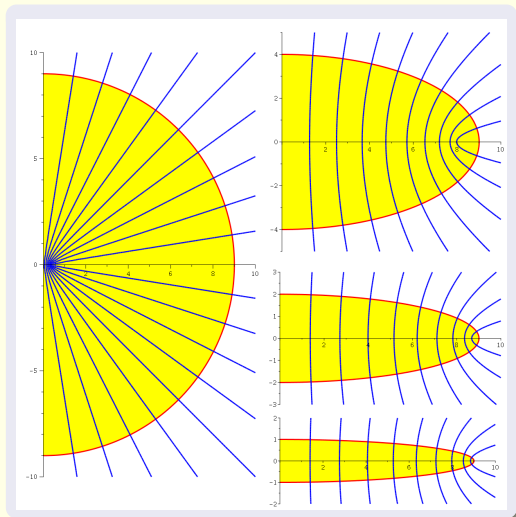
BACKUP SLIDES

1

Hyperbolic fieldlines

...at $t = 0$ allow for a smooth transition of geometry parameters from purely radial ($\propto \vec{e}_r$) to purely vertical ($\propto \vec{e}_z$).

- \vec{B} always \perp to ellipsoidal surface
- Field strength tunable on a per-fieldline basis.



MHD equations with turbulence

$$\partial_t \rho + \nabla \cdot (\rho \vec{U}) = 0$$

$$\partial_t (\rho \vec{U}) + \nabla \cdot \left[\rho \vec{U} \vec{U} + \left(\rho + \frac{|\vec{B}|^2}{2} + \rho_w \right) \mathbb{1} - \left(1 + \frac{\sigma_D \rho Z^2}{2B^2} \right) \vec{B} \vec{B} \right] = -\rho \vec{g}$$

$$\begin{aligned} \partial_t \mathbf{e} + \nabla \cdot \left[\mathbf{e} \vec{U} + \left(\rho + \frac{|\vec{B}|^2}{2} \right) \vec{U} - (\vec{U} \cdot \vec{B}) \vec{B} \right] + q_H - \frac{\rho H_c}{2} \vec{V}_A + \rho \vec{U} \cdot \vec{g} + \vec{U} \cdot \nabla \rho_w \\ = -(\vec{V}_A \cdot \nabla \rho) \frac{H_c}{2} + \frac{\rho Z^3 f}{2\lambda} + \vec{U} \cdot (\vec{B} \cdot \nabla) \left[\frac{\sigma_D \rho Z^2}{2B^2} \vec{B} \right] - \rho \vec{V}_A \cdot \nabla H_c \end{aligned}$$

$$\partial_t \vec{B} + \nabla \cdot (\vec{U} \vec{B} - \vec{B} \vec{U}) = \vec{0}$$

with $H_c \equiv \sigma_c Z^2$, $\rho_w = (\sigma_D + 1) \rho Z^2 / 4$, and $\sigma_D = \langle \delta u^2 - \delta b^2 / n \rangle / Z^2 = -1/3$.

The 3-eqn system, to be solved alongside the usual equations of ideal MHD (adapted from a talk by HF)

$$\partial_t Z^2 + \nabla \cdot (\mathbf{U}Z^2 + \mathbf{v}_A Z^2 \sigma_C) = \frac{Z^2(1-\sigma_D)}{2} \nabla \cdot \mathbf{U} + 2\mathbf{v}_A \cdot \nabla (Z^2 \sigma_C) + Z^2 \sigma_D \hat{\mathbf{B}} \cdot (\hat{\mathbf{B}} \cdot \nabla) \mathbf{U} \\ - \frac{\alpha Z^3 f^+}{\lambda} + \langle \mathbf{z}^+ \cdot \mathbf{S}^+ \rangle + \langle \mathbf{z}^- \cdot \mathbf{S}^- \rangle$$

$$\partial_t (Z^2 \sigma_C) + \nabla \cdot (\mathbf{U}Z^2 \sigma_C + \mathbf{v}_A Z^2) = \frac{Z^2 \sigma_C}{2} \nabla \cdot \mathbf{U} + 2\mathbf{v}_A \cdot \nabla Z^2 + Z^2 \sigma_D \nabla \cdot \mathbf{v}_A \\ - \frac{\alpha Z^3 f^-}{\lambda} + \langle \mathbf{z}^+ \cdot \mathbf{S}^+ \rangle - \langle \mathbf{z}^- \cdot \mathbf{S}^- \rangle$$

$$\partial_t (\rho \lambda) + \nabla \cdot (\mathbf{U} \rho \lambda) = \rho \beta \left[Z f^+ - \frac{\lambda}{\alpha Z^2} (\langle \mathbf{z}^+ \cdot \mathbf{S}^+ \rangle (1-\sigma_C) + \langle \mathbf{z}^- \cdot \mathbf{S}^- \rangle (1+\sigma_C)) \right]$$

with $f^\pm = \sqrt{1 - \sigma_C^2} \frac{\sqrt{1 + \sigma_C} \pm \sqrt{1 - \sigma_C}}{2}$, $\langle \vec{\mathbf{z}}^\pm \cdot \vec{\mathbf{S}}^\pm \rangle = \frac{(\partial_t Z^2)_{\text{pui}}}{2}$,

$$\vec{\mathbf{V}}_A = \vec{\mathbf{B}} / \sqrt{\rho}, \text{ and } \hat{\vec{\mathbf{B}}} = \vec{\mathbf{B}} / B$$