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# HADRONIC INTERACTIONS IN CRPROPA

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RUB



Cosmic Interacting Matters  
from source to signal



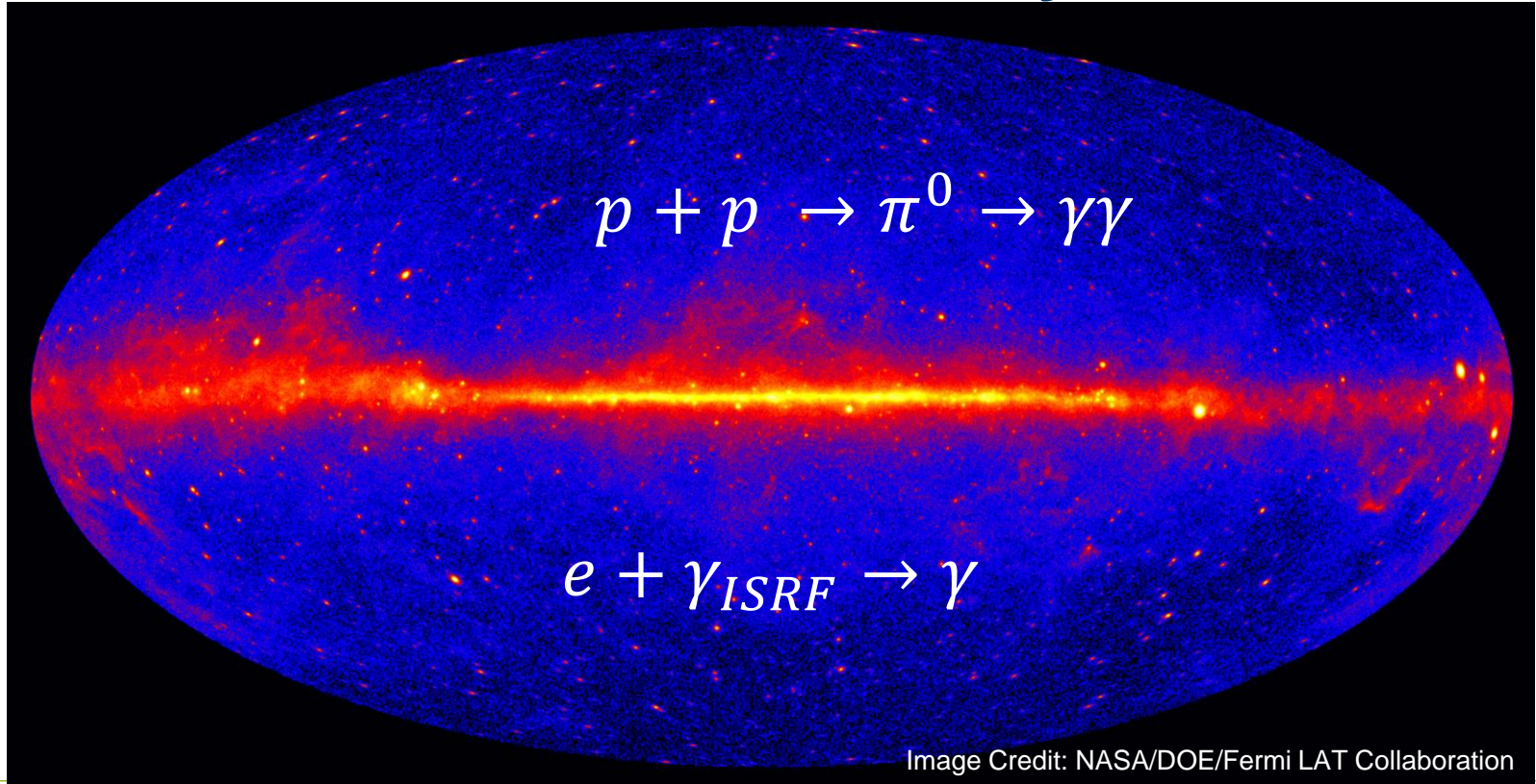
Funded by

**DFG**

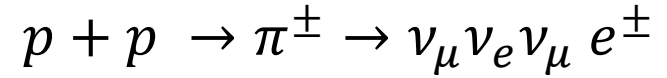
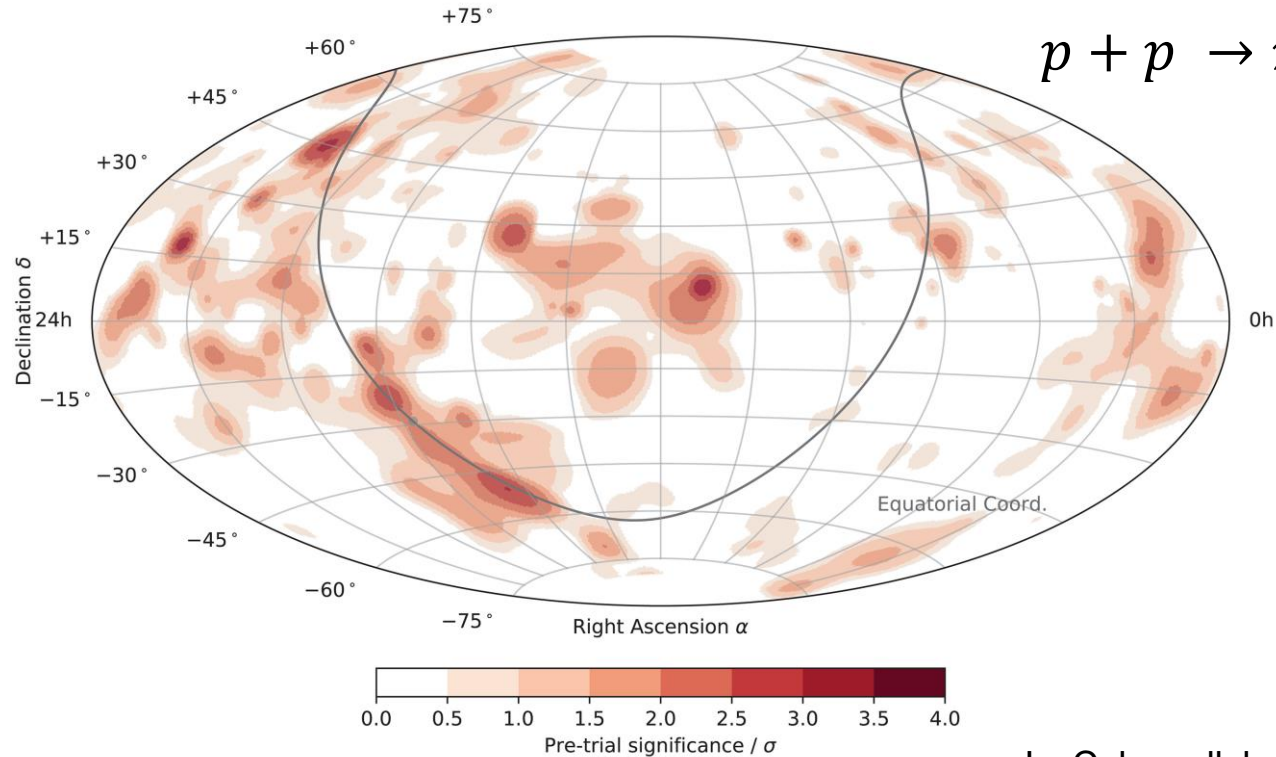
Deutsche  
Forschungsgemeinschaft  
German Research Foundation

**motivation**

# Impact of Galactic Cosmic Rays



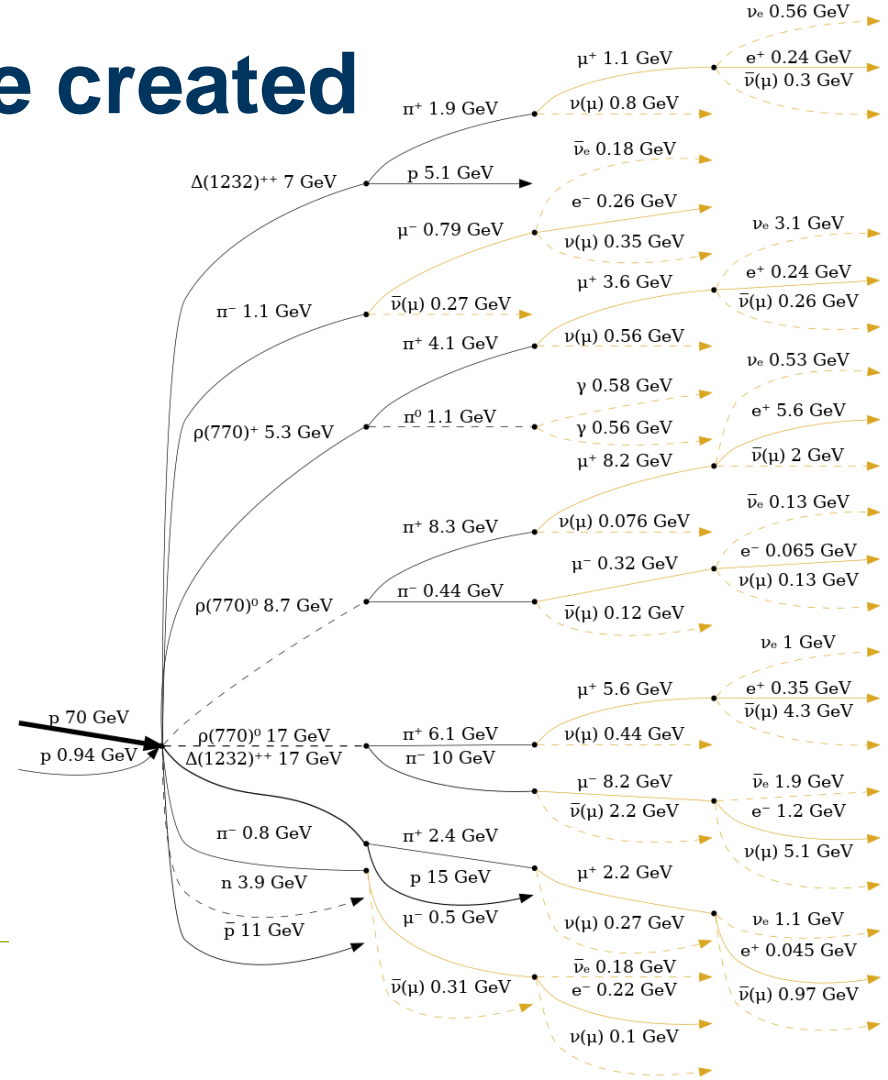
# Impact of Galactic Cosmic Rays



IceCube collaboration, Science 380, 6652

# bunch of particles can be created

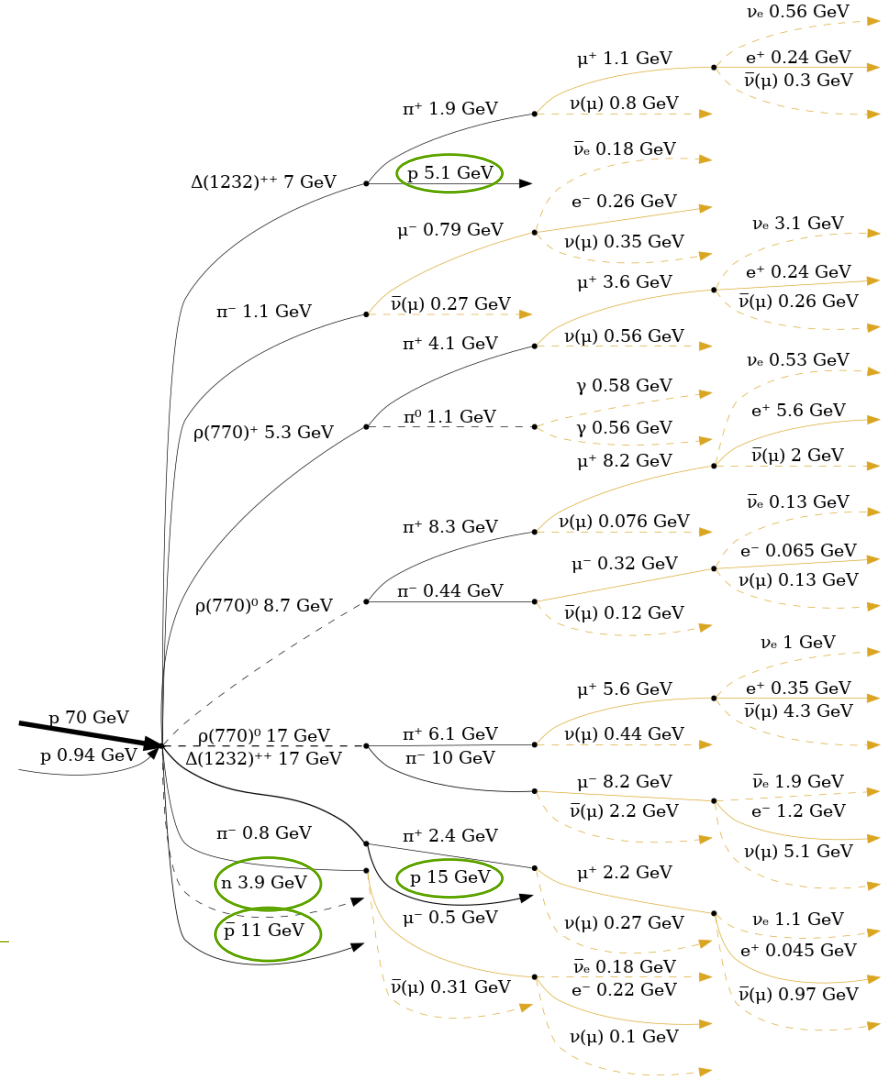
- $p + p \rightarrow \pi^0 \rightarrow \gamma\gamma$   
 dominant process for diffuse galactic gamma-ray emission
- $p + p \rightarrow \pi^\pm \rightarrow e^\pm \nu_e \nu_\mu$   
 production of (Galactic) neutrinos as seen in IceCube
- $p + p (A) \rightarrow \bar{p}, \bar{n}, \overline{He}$   
 seen by AMS-02



# Final state of interaction

- $e^-, e^+$
- $\nu_e, \bar{\nu}_e$
- $\nu_\mu, \bar{\nu}_\mu$
- $p, \bar{p}, n, \bar{n}$

includes up scattered proton and primary after interaction



# Crosssection models

# cross-section: inclusive and inelastic

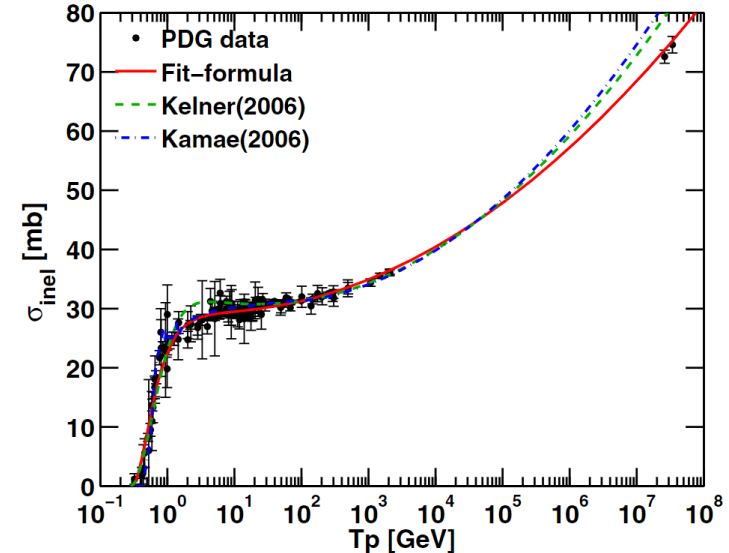
Inelastic cross-section: Kafexhiu+ (2014)

$$\sigma_0(T_p) = [30.7 - 0.96 \log(x) + 0.18 \log^2(x)] \times [1 - x^{1.9}]^3 \text{ mb}$$

$$x = \frac{T_p}{T_p^{th}} ; T_p^{th} = 2m_\pi + \frac{m_\pi^2}{2m_p} \approx 0.2797 \text{ GeV}$$

→ total interaction probability:

$$p = n_{gas} \cdot \sigma \cdot \Delta s$$





# cross-section: inclusive and inelastic

## Differential inclusive cross-section:

For each secondary species  $s$

$$\frac{d\sigma^{(s)}}{d\epsilon}(T_p, \epsilon) = \sigma_0(T_p) \cdot \frac{dN_s}{d\epsilon}$$

# Differential cross-section models - Kelner

**Paper:**

Kelner et al., PRD (2006) 034018, 74(3)

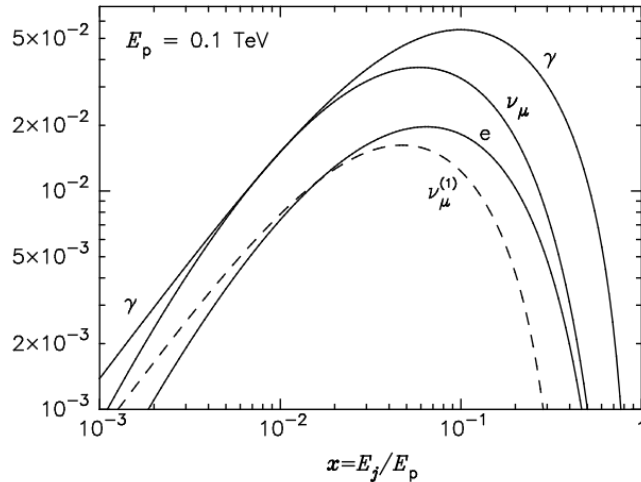
**Energy range:**

$100 \text{ GeV} < T_p < 10^5 \text{ TeV}$        $10^{-3} \leq \frac{\epsilon}{T_p} \leq 1$

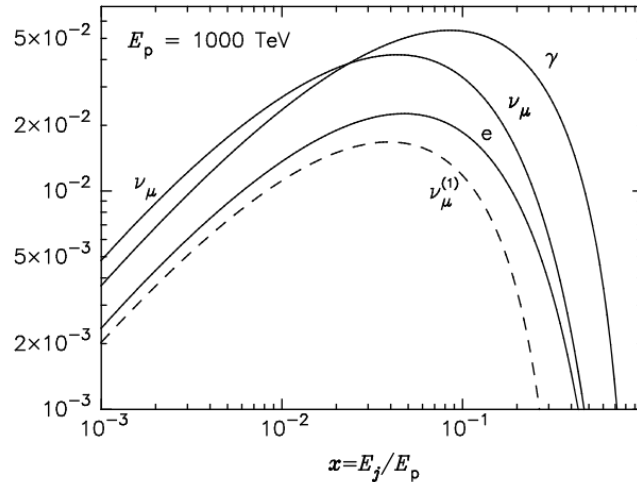
**Included secondaries:  
interaction:**

$e^\pm$  (one species),  $\nu_e$ ,  $\nu_\mu^{(1)}$ ,  $\nu_\mu^{(2)}$     **or**     $\pi^{\pm,0}$   
p-p

$x^2 F_j(x, E_p)$



$x^2 F_j(x, E_p)$



**RUB**

# Differential cross-section models - Kafexhiu

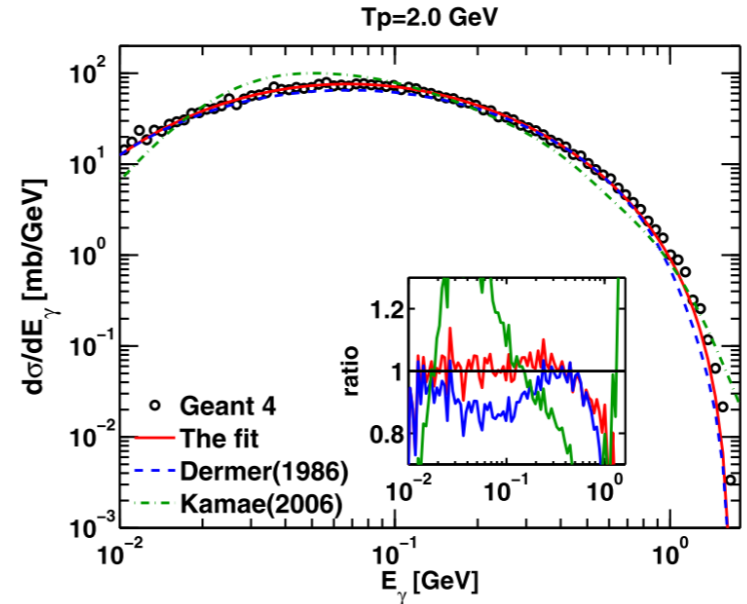
Paper:

Kafexhiu et al. PRD 90, 123014 (2014)

Included secondaries:  $\gamma$

interaction: p-p

- Includes the  $1\pi^0$  and  $2\pi^0$  channel
- Different parameters for different event generators



# Differential cross-section models - ODDK

<b>Paper:</b>	Orusa et al. (2022, 2023)
<b>Energy range:</b>	$100 \text{ MeV} < T_p^{(e)} < 10^3 \text{ TeV}$ $10 \text{ MeV} < \epsilon_e \leq 10 \text{ TeV}$ $100 \text{ MeV} < T_p^{(\gamma)} < 10^4 \text{ TeV}$ $10 \text{ MeV} < \epsilon_\gamma \leq 100 \text{ TeV}$
<b>Included secondaries:</b>	$e^\pm$ (separate), $\gamma$
<b>interaction:</b>	projectile: $^1\text{H}$ , $^2\text{H}$ , $^3\text{He}$ , $^4\text{He}$ , $^{12}\text{C}$ , $^{13}\text{C}$ , $^{14}\text{N}$ , $^{15}\text{N}$ , $^{16}\text{O}$ target: p, He

# Differential cross-section models - AAfrag

**Paper:**

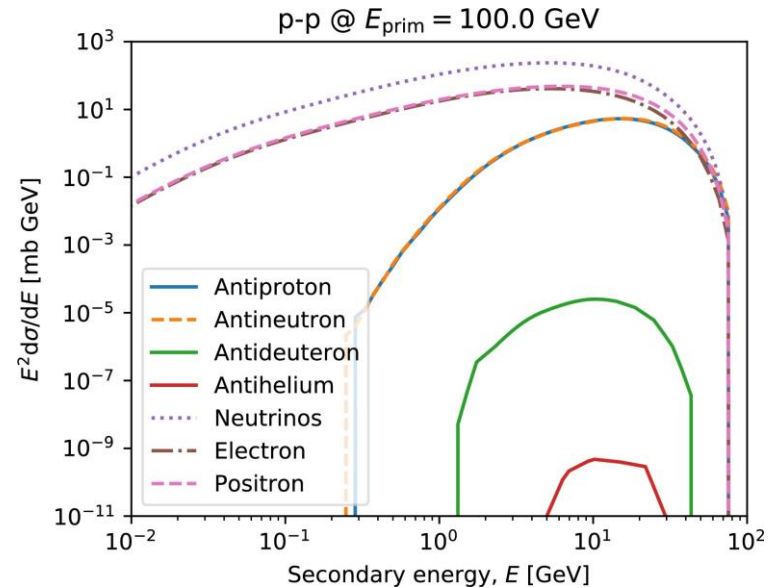
Kachelrieß et al, (2019), Computer Physics Communications, 245, 106846

**Included secondaries:**

$e^-$ ,  $\nu_e$ ,  $\nu_\mu$ ,  $\gamma$ ,  $p$ ,  $n$ ,  $\bar{d}$ ,  ${}^3\overline{\text{He}}$ ,  ${}^3\overline{\text{H}}$

**interaction:**

p-p, p-He, He-p, He-He, C-p,  
Al-p, Fe-p,  $\bar{p}$ -p,  $\bar{p}$ -p



# Comparison

# CRPropa Plug-In

# Precalculated data – for each secondary

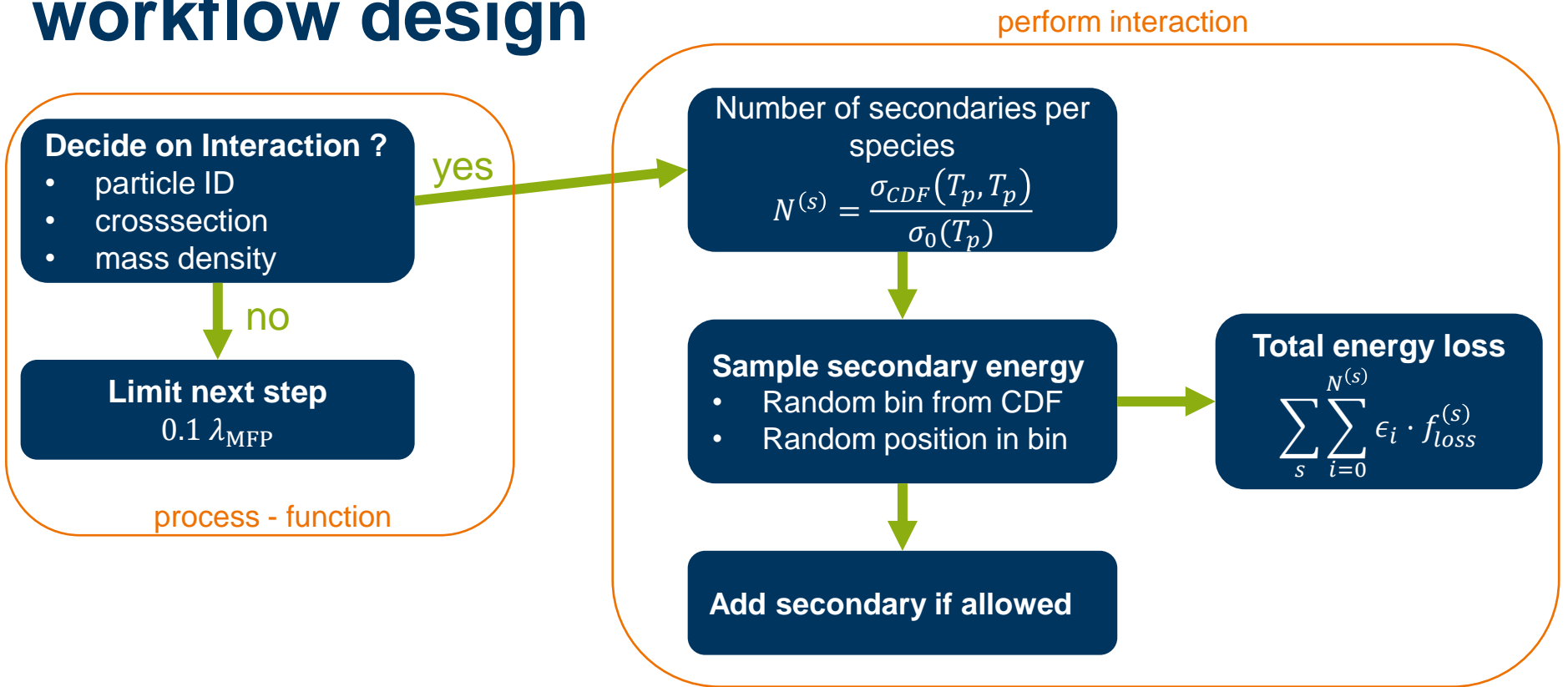
- 2D – table with a CDF

$$\sigma_{\text{CDF}}^{(s)}(T_p, \epsilon) = \int_{E_{th}}^{\epsilon} d\epsilon' \frac{d\sigma^{(s)}}{d\epsilon'}$$

- Correction factor for missing energy loss  $f_{loss}^{(s)}$
- Data are precalculated and collected with a config file
- Individual cross-section can be loaded and added to the module



# workflow design

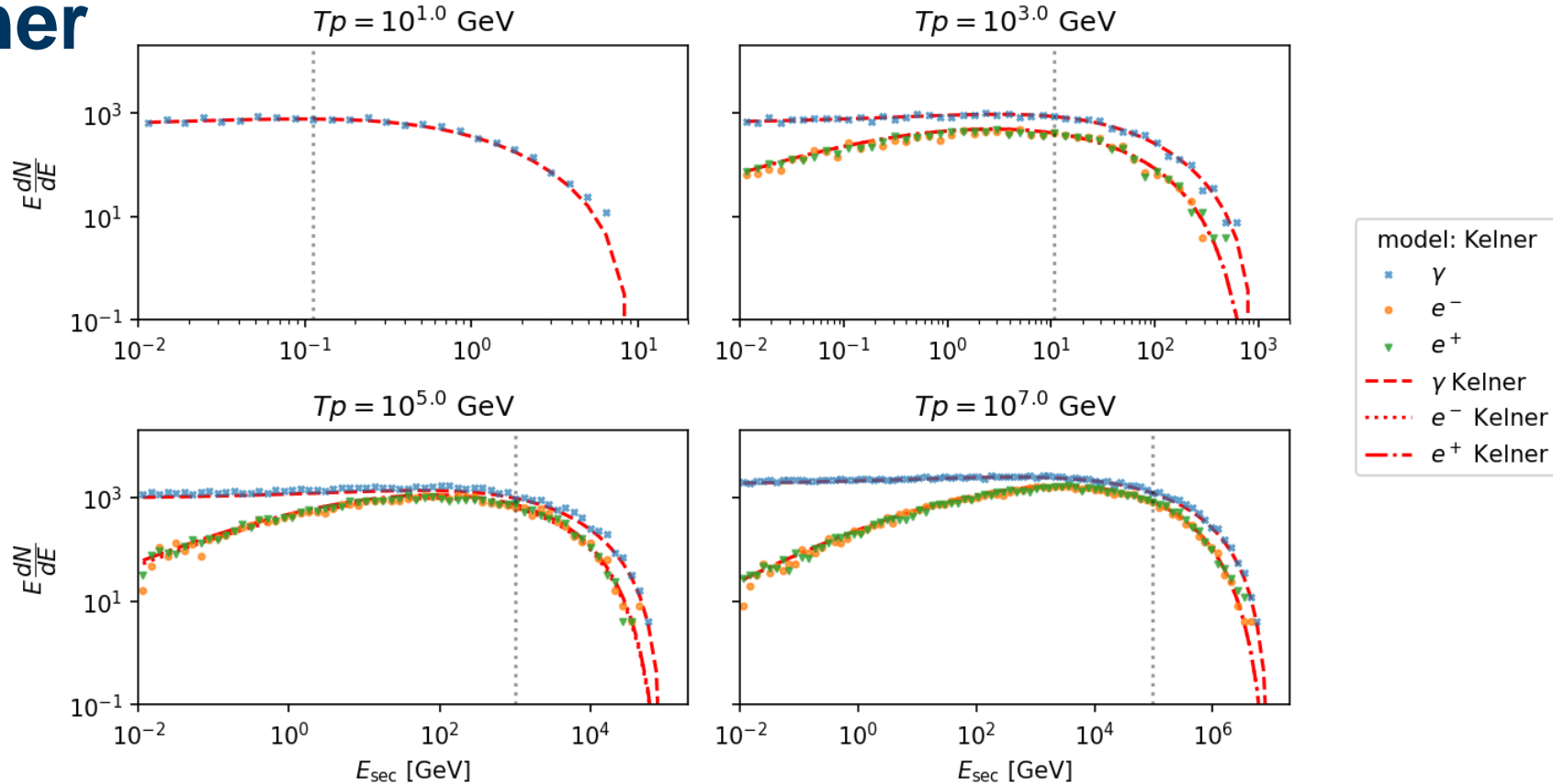


**testing**  
yields

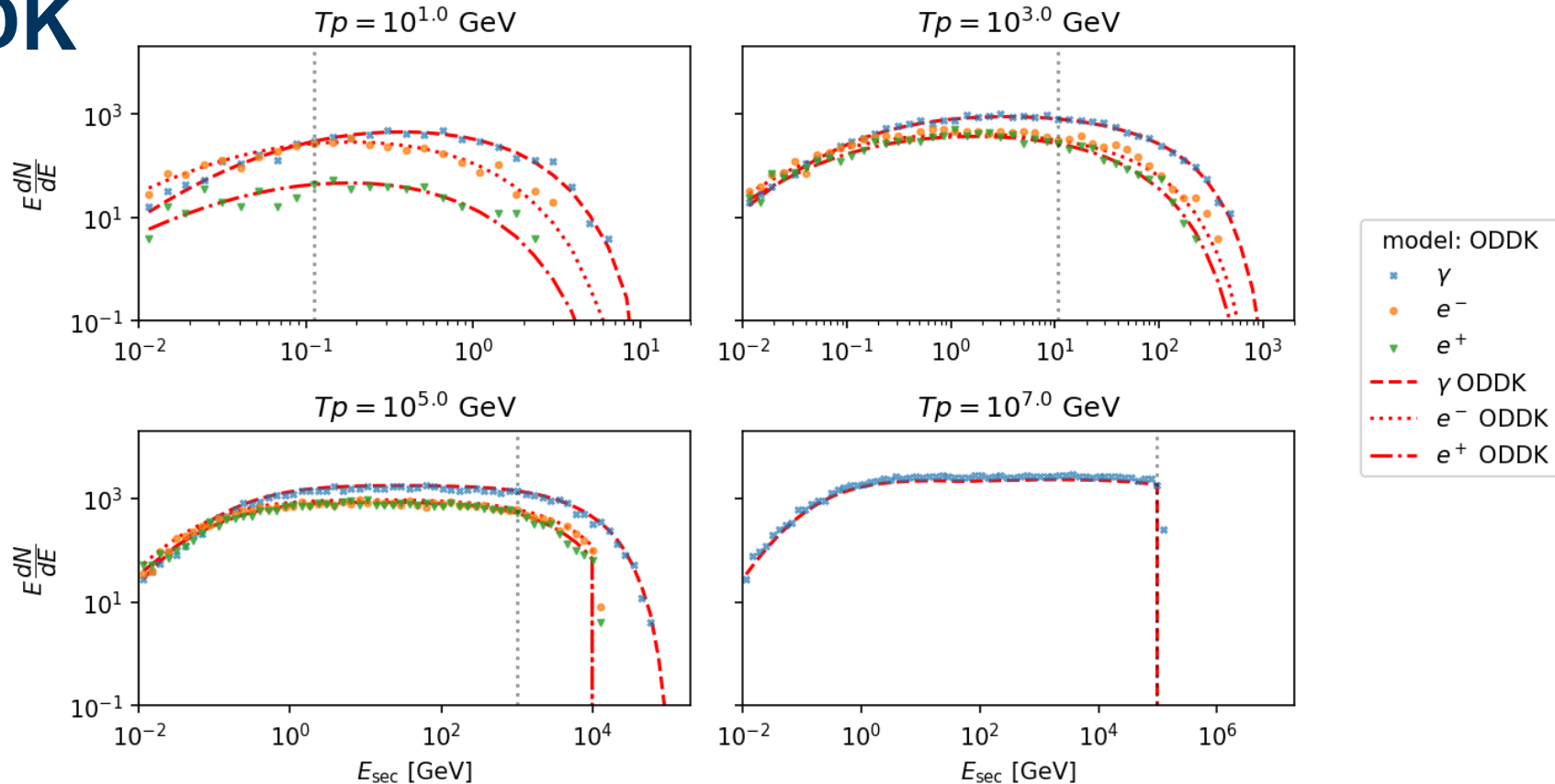
# Simulation setup for testing yields

- Fixed primary energy  $T_p$
- $10^5$  calls of `performInteraction`
- Calculate spectra of secondary particles
- Compare to shape of differential cross section (normed at  $10^{-2} T_p$ )

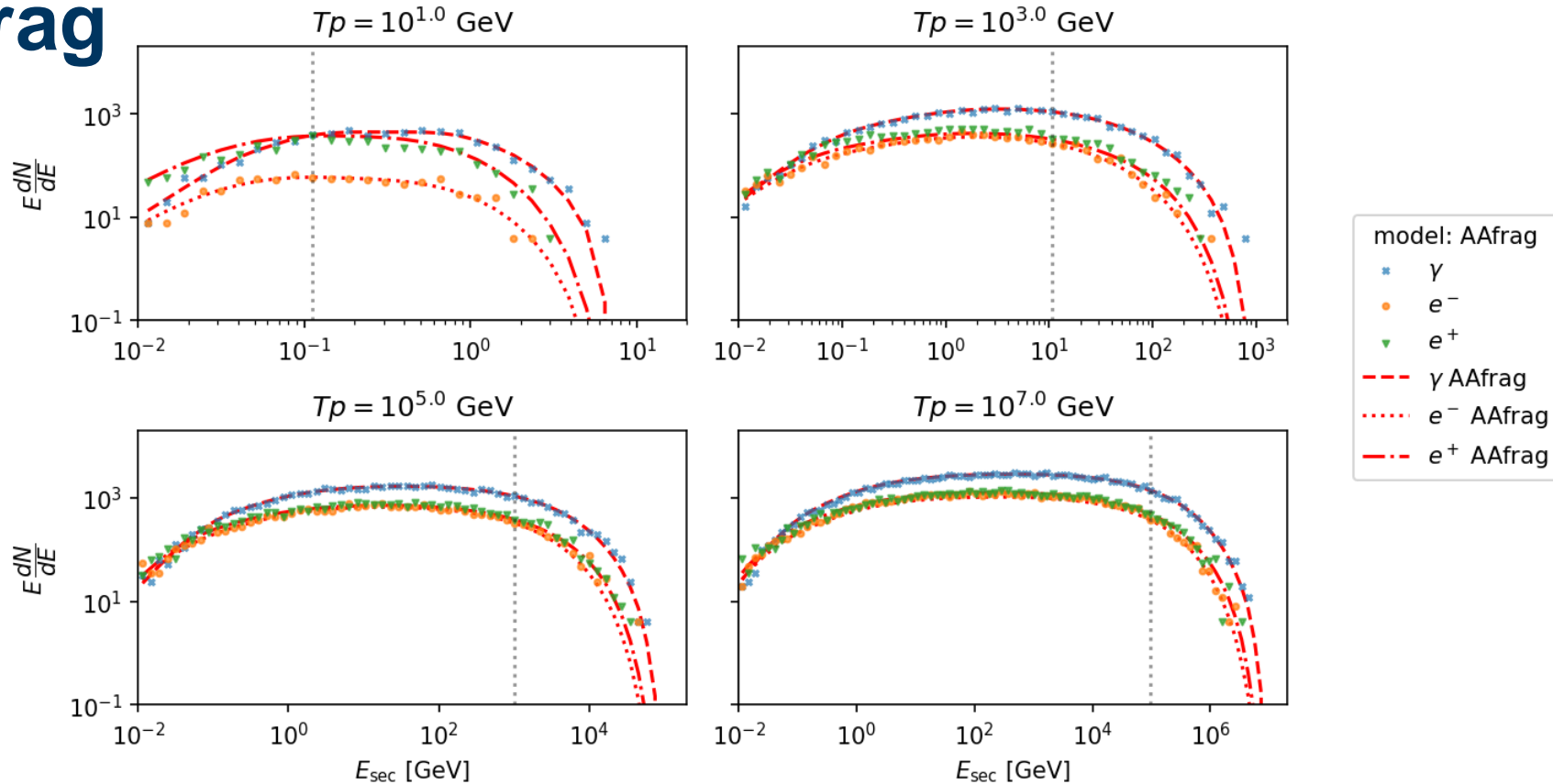
# Kelner



# ODDK



# AAfrag



**testing**

energy loss

# Energy loss from crossection

Total energy loss per unit time:

$$-\frac{dE}{dt}(T_p) = \int_{E_{th}}^{T_p} d\epsilon \ v \ \epsilon \ n(\vec{r}) \sum_s \frac{d\sigma^{(s)}}{d\epsilon}(T_p, \epsilon)$$

Approximation by Krakau & Schlickeiser (2015)

$$\frac{dE}{dt}(T_p) \approx 3.85 \cdot 10^{-16} \cdot \left( \frac{n}{10^6 \text{ m}^{-3}} \right) \cdot T_p^{1.28} \cdot (T_p + 200 \text{ GeV})^{-0.2} \text{ GeV/s}$$

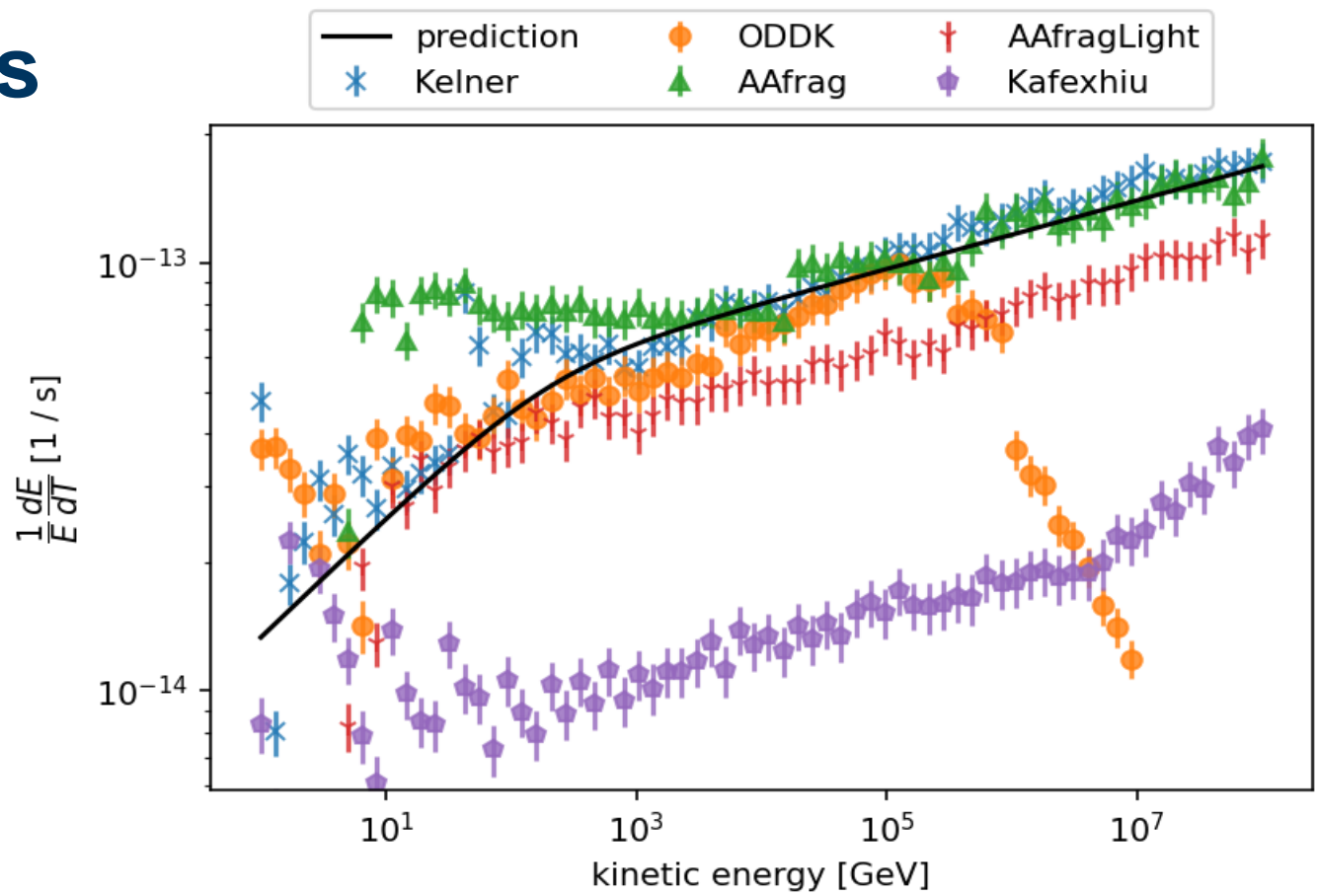


# Energy loss sampling

- $10^5$  particles per primary energy
- Primary (kinetic energy)  $1 \leq \frac{T_p}{\text{GeV}} \leq 10^8$  with 70 points in logspace
- Density  $n_H = 10^8 \text{ m}^{-3}$
- Propagate only one step with  $\Delta s = 0.01 \lambda_{\text{mfp}}$

$$\frac{dE}{dT} \approx \frac{\Delta E}{\Delta s/c}$$

# Energy loss



**application**

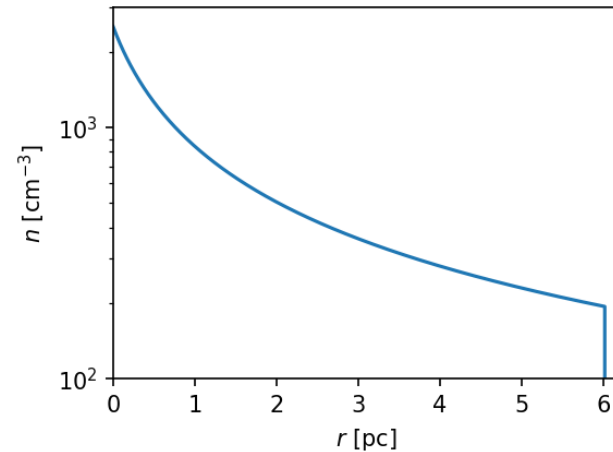
Giant Molecular Cloud

# Giant Molecular Cloud – Rho Oph

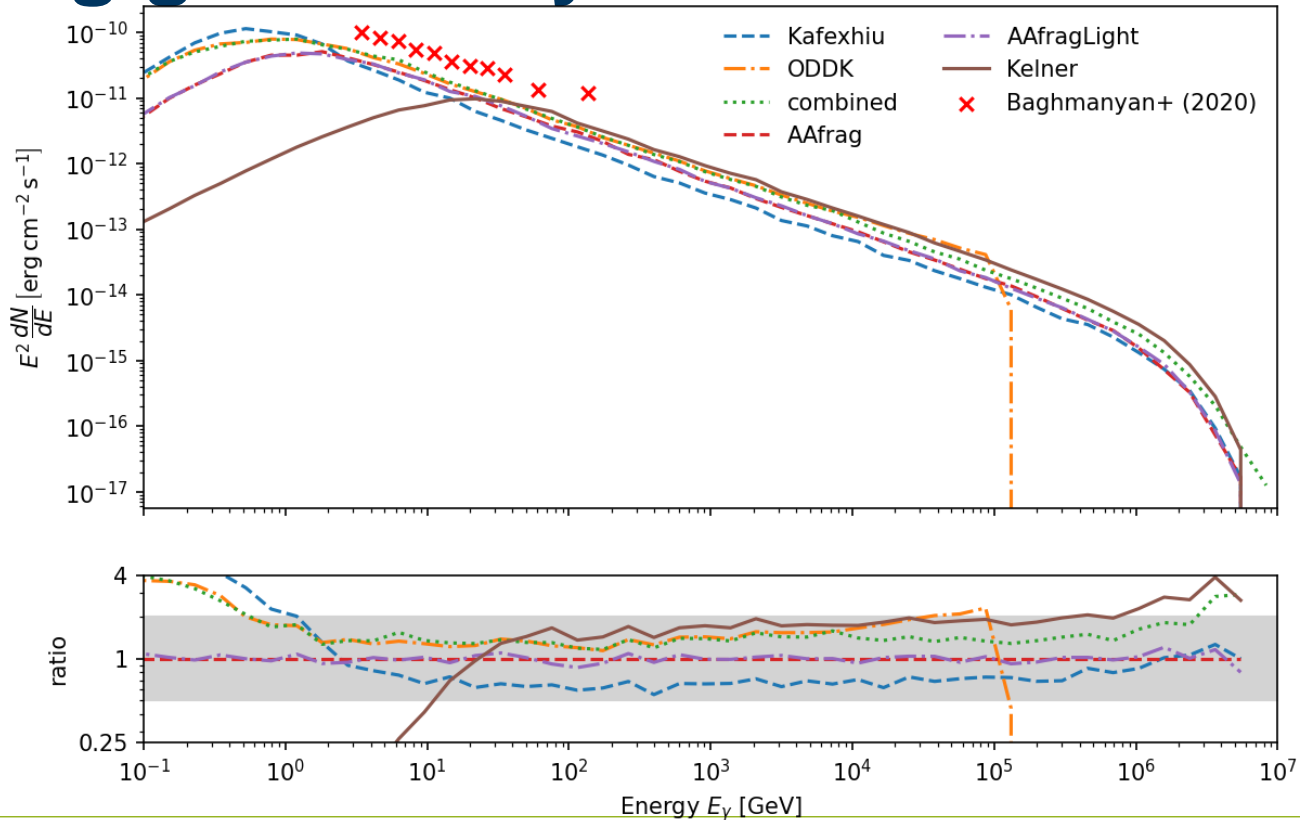


- Spherical dens cloud  $n(r) = \frac{n_0}{1 + \frac{r}{R_0}}$
- Injection on a sphere around the cloud
- $10^8$  particles with  $1 \text{ GeV} \leq T_p \leq 10^7 \text{ GeV}$
- Direct detection of created  $\gamma$ -rays
- Injection spectrum reweighted to LIS

$$\dot{j}_p(E) = 2.3 E^{1.12} \beta^{-2} \left( \frac{E + 0.67 \text{ GeV}}{1.67 \text{ GeV}} \right)^{-3.93} \frac{\text{particle}}{\text{GeV m}^2 \text{ s sr}}$$



# Resulting gamma-ray flux



**conclusion**

# Conclusion

- p-p interactions as a plug-in with custom secondaries
- Input: pre tabulated cross section for each secondary
- Tables available for: AAfrag, Kafexhiu, Kelner, ODDK
- Plug in tested for yields and energy loss
- results for different models with an uncertainty  $\sim 2$  for astrophysical application